

Hydrogen Bonding in the Mixed HF/HDCher: Is It Better to Give or Receive?

Sarah Niohnson and Gregory Schumpep*

The CIH FH and FH CIH configurations of the mixed HF/ more than 4 cm for the complexation induced HF frequency HCl dimer (where the donor acceptor notation indicates the CCSD(Telectronic energies obtained with the largdirectionality of the hydrogen bonds wellas the transition est basis set indicate that the barrier height is 0.400 kcal state connecting the two configurations have been optimated the FH CIH configuration lies 0.19 kmalf1 below the using MP2 and CCSD(With correlation consistent basis seldH FH configurationWhile only modestly attenuating the as large as aug-cc-pV(5 1 kd)Zmonic vibrationfeequencies barrierheight, the inclusion of either the harmonic on harconfirmed that both configurations correspond to minima remic zero-pointvibrational energy effectively makes both that the transition state has exactly one imaginary frequencyma isoenergetiwith the CIH FH configuration being In additionanharmonic vibratio frædquencies computed with ower by only 0.03 koao P1. ¥ 2018 Wiley Periodicans. second-order vibratioperturbation theory (VPTa2) within

6 cm²¹ of the available experimentables and deviate by no^{DOI:} 10.1002/jcc.25157

Introduction

The dimers resulting from the mono-hydratible and HCl gen halide donates the hydrogen bond to watermer configurations in which HF or HCcepts a hydrogen bond from orientation and strength of hydrogen bunds evealed that electronic structure methods his information indicates the infiguration? A subsequent heoretical nvestigation in (HF) and (HC) homogeneous dimers, 1st he mixed HF/HCl be approximately 0.5 kcar http://dispersion. dimer has received relatively little attention. This heterogence of the configurations emained isoenergetic afthere configuration was detected in the microwave specttbeof harmonic vibration adequency computations.contrast, he clearly indicate the directionality of the hydrogen Mored). tion was appreciably lower energy whethethe harmonic CIH FH configuration but also the FH CIH configuration imo²¹, respectivel³². That study also identified the correthe microwave and infrared (IR) ectra of molecular beams formed by expanding a mixture of HF and HCl in he he. authors inferred that the CIH FH configuration was lower vious paragraphs and provides reliable relative energetics for energy than the FH CIH configuration based on the relative

S.N.Johnson and G.Tschumper strengths of hyperfine transitions.1995Qudejans and Miller measured the dissociation energyofDthe mixed dimer using vibration**al**edissociation spectrosල් ම්මූ he වූ of the CIH FH configuration was determined to be 642 cm.84 kcal mol), however the for the FH CIH configuration was National Science Foundation Division of Chemistry Contractgrant not reported because it dissociates via a different pathwayuthaers1338056;664998 complicates such measurements.

In addition to these experimental studies, a variety of theoretical investigations have examined both configurations of this simple heterodimer. -22 Early self-consistent field (SCE) treeexhibit only a single low energy configuration, where the hydrocal computations by Kollman and co-workers compared different proton donors and acceptors to characterize the water have not been observed experimentally and do not rectionic energy of the FH CIH configuration was approxispond to minima when characterized sufficiently with robustely 1 kcmol1 higher in energy than that of the CIH FH although HF and HCl are good hydrogen bond donors, the your Latajka and Scheirier luded post-HF computations not be the best hydrogen bond acceptorsuchthe HF/HCl with second-order Møller-Plesset perturbation theory? (MP2). mixed dimer is an interesting system because hydrogen the computations indicated that the two configurations were formation requires one of the fragments to accept a hydragenergetic (within 0.1 kcall)mbi addition, a transition state bond from the otheDespite exhaustive work on the related nnecting the two configurations was identified and found to dimer was first characterized in 1900 only the CIH FH zero-point vibration enlergies (ZPVEs) were included from SCF molecular mechanics for clusters (MMC) method developed by donor acceptomotation has been adopted in this study taugspurger and Dykstra indicated that the FH CIH configurathan a decade late Fraserand Pine observed nobnly the ZPVE was included ont (by approximately 0.3 and 0.7 kcal sponding transition state with a barrier height of 0.형.kcal mol This study builds on the important work outlined in the pre-

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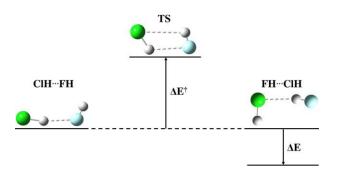


Figure 1.Depiction of the structure and energetic quantities sociate brary.com]

the two configurations blie mixed HF/HCdlimeras wellas the transition state barrileeight. The CCSD(T) method and only electronic energies near the complete basis set (CBS) binited from MP2 and CCSD(Toptimizations) iffer by no but also optimized geometribarmonic vibrationarequencies and anharmonic vibration fat quencies To the best of our knowledge he results presented here include (i) first ture methods(ii) the firstab initio harmonic vibrationfedquencies beyond the SCF leveltheory and (iii) he firstab initio relative electronic energibesyond the MP2 computabonding prototypeThe data presented here anchotisese the HF/HCdimer system.

Methodology

connecting the two have been optimized usifig MR2 the CCSD(T)coupled clustemethod thatincludes alkingle and double substitutions as weedla perturbative estimate los connected triple substitutions with a series of orrelation consistent basis sets augmented with diffuse functions on leave from the consistent basis sets augmented with diffuse functions on leave from the consistent basis sets augmented with diffuse functions on leave from the consistent basis sets augmented with diffuse functions on leave from the consistent basis sets augmented with diffuse functions on the consistent basis sets augmented with diffuse functions on the consistent basis sets augmented with diffuse functions on the consistent basis sets augmented with diffuse functions on the consistent basis sets augmented with diffuse functions on the consistent basis sets augmented with diffuse functions on the consistent basis sets augmented with diffuse functions on the consistency of the consisten (cc-pVXZ forH, aug-cc-pVXZ forF, aug-cc-pV(X 1 d)Z fort, (DE) is slightly small (0.4 kcamo^{21}) at the CCSD(T) evel where X 5 DT, Q and 5; denoted ha(X 1 d) 20.321 Harmonic of theoryBoth harmonic and anharmonic ZPVEs attenuate the vibrationarequencies confirmed that both configurations sarrier to a small degree. respond to minima and that the transition state has exactly able 3 reports the dissociation energies both minima imaginary frequency on both the MP2 and CCSDD(TE)ntial computed with the ha(5 1 d)Z basis Weth this large basis energy surfaces harmonic vibration adquencies were com-set, the Boys-Bernardounterpoise procedure (CIP) creases puted using MP2 and CCSD(With second-orderibrational the MP2 and CCSD(Te)lectronic dissociation energy) (Dalresonances were detected at any dethetory for either con-dure has an even small effect (0.04 kcal mol²) on the figuration othe transition state. 361 The MP2 optimizations relative dissociation energi@D) which suggests that the out with Gaussian $\theta \theta$ whereas a (CCSD(T) computations and where the inconsistency commonly referred to basis set VPT2 analyses were performed with CFOUR.

Results and Discussion

The two different configurations be mixed dimeand the transition state connecting them can be seen in Figure 1.for the CIH FH configuration by Oudejans and Miler.

CIH FH configuration has Hacting as the hydrogen bond donorwhile HF acts as the acceptorhereas the situation is reversed fothe FH CIH configurationThe structure of the transition state closely resembles a parallelogram but is technically an irregular convex quadrilateenmetricadarameters for the different configuration and the transition state are reported in Table The intermolecular distances (R(H A) and R(D A) in Table 1, where A stands for acceptor and D stands for donor)obtained from MP2 and CCSD6Dtimizations are remarkablysimilarand in good agreement with available experimentahtermoleculadistances (within 2%) long as with the mixed HF/H6Imer[Color figure can be viewed at wileyonlineX-5 TQ or 5.Deviations are somewhat larger for the intermolecular anglebut that is not too surprising given the floppy nature of the system and some of the approximations invoked to obtain the experimentally inferred geometrical meters. Although no experimentatramolecular distances (Ráfid) large correlation consistent basis sets are used to compute (CIPI) in Table 1) are available the corresponding values more than 0.5% forboth configuration and the transition state when X 5 \overline{\Pi}. or 5.

Energies relative to the CIH FH configuration are depicted in anharmonic vibrational alysis with ab initio electronic struggure 1 and reported in Table 2. The energy difference between the CIH FH and FH CIH configurations is given by the DE term, while DE represents the energy difference between the transition state and the CIH FH configuration.electronic tions from Latajka and Scheinter this important hydrogenenergy of the FH CIH configuration is lower than the CIH FH configuration by approximately 0.2 kcalwheln X 5 TQ or three key stationary points on the poteential gy surface of 5 with either the MP2 or CCSD(Te) thod as indicated by the DE values in the DE columns Table 2. The ZPVE effectively eliminates the energetic separation of the two miaking both configurations essentially isoenergetic when either the harmonic or anharmonic ZPVEs are includeth (i. D₽ and D₽ Both configurations of the HF/HCl dimer and the transition state in Table respectively CSD(T) computations with the ha(Q 1 d)Z and ha(5 1 d)Z basis sets indicate that the FH CIH configuration is only 0.03 kmalf¹ higher in energy than the CIH FH configuration when anharmonic ZPVEs are included. For the transition state (DELIMING of data in Table 2), the MP2 hydrogen atoms and an extra set of tight d functions for above the CIH FH configuration barrier height

perturbation theory (VP†2)No Fermior Darling-Dennison ues by no more than 0.1 kaa6p1. The counterpoise proceand harmonic vibratiofrequency computations were carribe (5 1 d)Z energetics reported here are close to the CBS limit, superposition error (BSSE) vanishes by definite ionarmonic

or anharmonicZPVEs decrease the dissociation energby slightly more than 1 kcabp1. The MP2 and CCSD(T) Dalues of 1.87 and 1.81 kcmlo²¹, respectively re in excellent agreement with the 1.84 kmal¹ experimental obtained



Table 1.Geometricalarameters (distances \mathring{R} and less hin degrees and the average rotation along R_{K}) in MHz) for the different configurations of the mixed HFditGer and the transition state (TS). (Righere D and A denote the halogen atoms associated with the hydrogen bond donor and acceptospectively.

Config.	Levelof theory	R(FH)	R(CIH)	R(H A)	R(D A)	h(D A-H)	B_K
CIH FH	MP2/ha(D 1 d)Z	0.926	1.287	2.07	3.35	119.6	3479
	MP2/ha(T 1 d)Z	0.924	1.277	2.06	3.32	116.0	3537
	MP2/ha(Q 1 d)Z	0.921	1.277	2.04	3.31	116.3	3568
	MP2/ha(5 1 d)Z	0.920	1.277	2.04	3.31	116.3	3573
	CCSD(T)/ha(D 1 d)Z	0.925	1.290	2.10	3.38	119.5	3412
	CCSD(T)/ha(T 1 d)Z	0.923	1.280	2.08	3.35	115.2	3490
	CCSD(T)/ha(Q 1 d)Z	0.920	1.280	2.06	3.33	115.3	3523
	CCSD(T)/ha(5 1 d)Z	0.919	1.280	2.06	3.33	115.2	3528
	Experiment[s]	_	-	2.08	3.37	130.0	3422
FH CIH	MP2/ha(D 1 d)Z	0.929	1.285	2.38	3.30	90.4	3673
	MP2/ha(T 1 d)Z	0.927	1.275	2.31	3.23	90.7	3825
	MP2/ha(Q 1 d)Z	0.924	1.275	2.32	3.23	89.8	3828
	MP2/ha(5 1 d)Z	0.924	1.274	2.31	3.23	89.5	3839
	CCSD(T)/ha(D 1 d)Z	0.928	1.289	2.40	3.32	91.0	3634
	CCSD(T)/ha(T 1 d)Z	0.926	1.279	2.32	3.24	91.1	3795
	CCSD(T)/h@(1 d)Z	0.923	1.279	2.33	3.24	89.9	3796
	CCSD(T)/ha(5 1 d)Z	0.922	1.278	2.33	3.24	89.6	3806
	Experiment[s]	_	-	2.36	3.28	93.0	3710
TŚ ^a l	MP2/ha(D 1 d)Z	0.927	1.286	2.53	3.25	55.2	3798
	MP2/ha(T 1 d)Z	0.924	1.276	2.44	3.23	56.2	3840
	MP2/ha(Q 1 d)Z	0.921	1.276	2.41	3.22	57.4	3861
	MP2/ha(5 1 d)Z	0.921	1.275	2.40	3.21	57.4	3875
	CCSD(T)/ha(D 1 d)Z	0.925	1.289	2.53	3.26	56.6	3771
	CCSD(T)/ha(T 1 d)Z	0.923	1.279	2.44	3.23	56.9	3832
	CCSD(T)/ha(Q 1 d)Z	0.920	1.279	2.41	3.22	58.4	3854
	CCSD(T)/ha(5 1 d)Z	0.920	1.279	2.40	3.22	58.4	3868
[a] The TS d	ata corresponds to when a r	Ed CA 5 F.					

The harmonic vibratiofrequencies for both configuration (Q 1 d)Z and ha(5 1 d)Z frequencies is $^{2}1$ from both the and the transition state are reported in the supplementar MP2 and CCSD(Tr)nethodsIn light of these smaller viations informationThe imaginary mode tife transition state has aand the computationademandsof the CCSD(T)/ha(5 1 d)Z magnitude of 137 2 mat the CCSD(T)/ha(5 1 d)Z left theory and corresponds to the in-plane rocking motioboth hydrogenswhich leads downhild eitherconfiguratiorHarmonic frequencies computed with the ha(Q 1 d)Z basiset ha(5 1 d)Z values r the eighteen modes associated with the comparison to the available experimental stretching

Table 2.Relative electronic energies (DMI zero-point corrected relative energies using harmon\\ \alpha \text{dDE} anharmonic \(\bar{D}\text{E}ibrationa \) frequencies, here alquantities are in know f1 and relative to the CIH FH configuration.

		М	P2	CCSD(T)		
Basis set		DE	DÉ	DE	DÉ	
ha(D 1 d)Z	DE	10.09	10.61	10.02	10.54	
	DE	10.29	10.44	10.24	10.43	
	DE	10.30	10.49	10.24	10.49	
ha(T 1 d)Z	DĘ	20.19	10.53	20.22	10.45	
	DĘ	10.07	10.34	10.05	10.33	
ha(Q 1 d)Z	DE₀	10.06	10.38	10.02	10.39	
	DE₀	20.16	10.50	20.19	10.41	
	DE₀	10.06	10.34	10.03	10.31	
ha(5 1 d)Z	DE	10.06	10.36	10.03	10.37	
	DE	20.17	10.48	20.19	10.40	
	DE	10.05	10.34	10.02	10.25	
	DE	10.06	10.36	10.03 ^a]	10.36 ^a]	
[a] Anharmonic correction from ha(Q 1 d)Z.						

Hessians he CCSD(T)/ha(Q 1 d)Z VPT2 results are being used as proxies for the corresponding ha(5 1 d)Z Values harmonic frequencies and IR intensities for both minima are reported in the supplementarinformation along with the neverdeviate by more than 6 2th from the corresponding complexation induced donor and acceptor frequency shifts. three structures average absolute deviation between three quencies (rand shifts induced by hydrogen bond forma-

> tion (Dmare given in Table 4For the CIH FH minimum in which HF acceptshe hydrogen bond from HCthe anharmonic CCSD(T)/ha(Q 1 d)Z frequencies from the VPT2 computations are within 2 cm of the experimental f stretching

Table 3.Electronic dissociation energies (Camo²¹), counterpoise corrected electronic dissociation energies (Dalmof1), zero-point corrected dissociation energies using harmanik (amof1) and anharmonic (In kcamof1) vibrational equencies and relative dissociation energies (DD in knaf1) characterized with the ha(5 1 d)Z basis set.

	MP2			CCSD(T)			
	CIH FH	FH CIH	DD	CIH FH	FH CIH	DD	
D _e	2.84	3.01	20.17	2.76	2.95	20.19	
D _e D _e D _o	2.78	2.91	20.13	2.71	2.88	20.17	
Dh	1.71	1.66	10.05	1.63	1.61	10.02	
D_0	1.87	1.81	10.06	1.8 1 a]	1.78 ^a]	10.03 ^a	
[a] Anharmonic correction from ha(O 1 d)7.							



Table 4.Harmonic vibrational quencies (xin cn²¹) and VPT2 anharmonic correction (th cn²¹) at different levels of theory are combined to obtain anharmonic vibraHorsaretching frequencie (Dm in chh).

Harmonic	VPT2	Хe	d^{anh}	m	Dm	
CIH FH						
MP2/ha(Q 1 d)Z	MP2/ha(Q 1 d)	Z4106	2170	3936	227	
MP2/ha(5 1 d)Z	MP2/ha(5 1 d)	Z 4106	2171	3935	228	
CCSD(T)/ha(Q 1 d	I)ZMP2/ha(Q 1 d)	Z4116	2170	3946	217	
CCSD(T)/ha(5 1 d)ZMP2/ha(5 1 d)	Z 4117	2171	3946	215	
CCSD(T)/ha(Q 1 d)ZCCSD(T)/	4116	2174	3942	221	
	ha(Q 1 d)Z					
CCSD(T)/ha(5 1 d)ZCCSD(T)/	4117	2174	3943	220	
	ha(Q 1 d)Z					
Experiment [15]				3940	221	
FH CIH						
MP2/ha(Q 1 d)Z			2158	3850	2113	
MP2/ha(5 1 d)Z	,		2159	3849		
CCSD(T)/ha(Q 1 d	l) Z MP2/ha(Q 1 d)	Z 4032	2158	3874	289	
CCSD(T)/ha(5 1 d)ZMP2/ha(5 1 d):	Z 4031	2159	3872	289	
CCSD(T)/ha(Q 1 d	I)ZCCSD(T)/	4032	2159	3873	290	
	ha(Q 1 d)Z					
CCSD(T)/ha(5 1 d)ZCCSD(T)/	4031	2159	3872	291	
ha(Q 1d)Z						
Experiment [15]				3867	294	

frequency.Interestinglythe correspondingMP2/ha(Q 1 d)Z overlapping Lorentzian functions with a which halfmaxitions from the experimentalstretching frequency are someussed in detail the last section of Ref5] what larger when HF donates the hydrogen bond in the FH CIH configuration. The CCSD(T)/ha(Q 1 d)Z resistatill within 6 cm 1 , but the differences grow as large as 18^{1} cm. This work provides the firthtorough characterizationths for the anharmonidMP2 frequenciescomputed with the ha(Q 1 d)Z and ha(5 1 d)Z basis sets.

To shed more light on this situatiting harmonic (a) and the MP2 and CCSD(T)anharmonicontributions the HF stretching frequencies are nearly identiorathe more challenging HF donothe danh terms differ by only 1 chwhich indicates the large MP2 deviation from experiment the

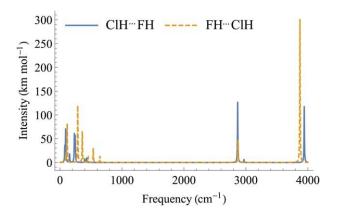


Figure 2.Simulated anharmonic vibratispectra of both the CIH FH and FH CIH configurations the CCSD(T)/ha(Q 1 d)Z leveltheory. [Color figure can be viewed at wileyonlinelibrary.com]

FH CIH configuration can be attributed to the harmonic component of the vibrationa frequency In fact, the same good agreement with the experimentaltretching frequen-(m in cm) and complexation induced anharmonic HF frequency shifts and frequency shifts can be obtained by combining the CCSD(T)harmonicfrequencies with the anharmonic orrections from MP2 VPT2 computations.

> The CCSD(T)/ha(Q 1 d)Z anharmonic vibratipeatra for both configurations can be seen in FigureO2vertones and combinationbands with up to three vibrational quanta (ml m5 3) are included in the spectra and also tabulated in the supporting information wevermost do not have sufficient IR intensity to be visible on this street emovertone at 537 cm²¹ has the greatesintensity but is still only 30 km mo²¹. Both configurations have numerous low-energy fundamentamodes under 500 2 mwith more significant IR intensities on the order of 100 km²h.dHoweverthe HF and HCl stretching modes between 2800² chand 4000 cm² have the largestintensities or both configuration \$100-300 km mo²¹). For the CIH FH configuration the HF and street. ing modes have similar intensitibere the FH ClH configuration showcases HF stretchingmode as the most intense peak which is three times lathen any other peak in eitherspectrumIt is importanto note thatthe peaks in the simulated spectra shown in Figure 2 were generated by

and MP2/ha(5 1 d)Z anharmonic frequencies are quite similar value of 4 ch whereas the experimentaks exhibit and lie within 5 cm of the experimentablue. These devia- significant broadening from vibration as dis-

Conclusions

system (via fullgeometry optimizations d vibrationa frequency analysewith correlated ab initio methods and large anharmonic (d) components ofhe VPT2 frequencies have bound by almost3 kcal mol² nearthe CCSD(T)/CBS limit. been listed separately in Table ith the ha(Q 1 d)Z basis set the CCSD(T)/ha(5 1 d)Z electrodissociation energies response to the CCSD(T)/ha(5 1 d basis setsBoth configurations to mixed HF/HCdimer are 2.76 kcalmo^{P1} for the CIH FH minimum and 2.95 kcal mol²¹ for the FH CIH minimum. The values decrease by 0.05 and 0.07 kcamo^{P1} respectively when the CP procedure is applied. The relative CCSD(T)/ha(5 1 d)Z electromiergies show that the FH CIH configuration is lower than the CIH FH configuration by 0.19 koab^{P1} and that the transition state is 0.40 kcab^{P1} higher than the CIH FH configuration. However, the inclusion of either the harmonicor anharmoni&PVE makes both minima isoenergeti&within 0.03 kcaho²¹ of each other according to the CCSD(T) results obtained with the two largest basis stetes ZPVE corrections also decrease the barriemeight by approximatel 9.1 kcal mo²¹. The CCSD(T)/ha(Q 1 d)**Zf**or the CIH FH configuration deviates from the experimental alue by 20.03 kcal mo^{2} . The CCSD(T)/ha(Q 1 d)Z anharmonic frequencies complexation induced frequency shifts differ by no more than 26 cm²¹ from the experimentælue^[15]To concludethese computations indicate thatere is a slightelectronic preference for HF to donate and H6laccept a hydrogen bond in this mixed dimer.hat proclivity vanishas, weverwhen the



ZPVE is included which suggestgiving and receiving are [13]H. Jiang,A. SarsaG. MurdachaewK. Szalewic Z. Bačć, J. ChemPhys. equally virtuous in this confexe relative energetics indicate 2005,123224313.

both configurations of the mixed HEMIChr should be pro [14]K. C. Janda, J. M. Steed, S. E. Novick, W. Klemperey, Chem. Phys. both configurations of the mixed HFdHGer should be present in experiments conducted at extremely low temperationless. FraserA. S. Pine, J. ChemPhys1989 91,637. and pressures The CCSD(T)/ha(Q 1 d)Z anharmonic freque $\frac{1}{10}$ L. Oudejans. E. Miller J. Phys. Chem 1995, 99, 13670. cies reported here from VPT2 computations reidtly facilitate more complete assignment the vibration appectra of [18]P. Kollman J. McKelvey A. Johansson S. Rothenberg, Am. Chem Soc. these two minimaoth of which have multiple fundamentals 1975,97,955. with appreciable IR intensities asawellvertones and combi [19]P. KollmanJ. Am. ChemSoc 1977,99,4875. nation bands below 600 ²Cnthat willlikely be discernible in [21]Z.Latajka\$. ScheineChemPhys1988,122413. their IR spectra.

Acknowledgments

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Professor John Stanton at University of Florida is thanked for York 1970. resolving issues regarding VPT2 computations for transition states heoryWiley-Interscience York1986. Dr.J. Coleman Howard at Virginia Terchhomas Mexton at [27]C. Møller M. S. Plesset Phys Rev. 1934, 46, 618. University of Mississippi, and Dr. Louis E. McNamara at Ufflyers Ret let Ann. Rev. Phys. Chem. 1981, 32,359.

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Mississippi are thanked for helpful discussions and technical Experiments. Chem. Phys. 1989, 90,1007. computations and literature review.

Keywordshydrogen bondingdissociation energiesoupled cluster method (CCSD(To)) mplete basis set (CBS) limitond-order vibration red rturbation theory (VPT2)

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- Additiona Supporting Information may be found in the online version of this article.
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